

# Photometric study of three ultrashort-period contact binaries in different special evolutionary stages

L. Liu<sup>1,2,3,4</sup>, S.-B. Qian<sup>1,2,3,4</sup>, E. Fernández Lajús<sup>5,6,†</sup>, A. Essam<sup>7</sup>, M. A. El-Sadek<sup>7</sup>, and X. Xiong<sup>1,2,3,4</sup>

## ABSTRACT

We carried out high-precision photometric observations of three eclipsing ultrashort-period contact binaries (USPCBs). Theoretical models were fitted to the light-curves by means of the Wilson-Devinney code. The solutions suggest that the three targets have evolved to a contact phase. The photometric results are as follows: a) 1SWASP J030749.87–365201.7,  $q = 0.439 \pm 0.003$ ,  $f = 0.0 \pm 3.6\%$ ; b) 1SWASP J213252.93–441822.6,  $q = 0.560 \pm 0.003$ ,  $f = 14.2 \pm 1.9\%$ ; c) 1SWASP J200059.78+054408.9,  $q = 0.436 \pm 0.008$ ,  $f = 58.4 \pm 1.8\%$ . The light curves show O’Connell effects, which can be modeled by assumed cool spots. The cool spots models are strongly supported by the night-to-night variations in the *I*-band light curves of 1SWASP J030749.87–365201.7. For a comparative study, we collected the whole set of 27 well-studied USPCBs with  $P < 0.24$  day. Thus, we found that most of them (16 of 27) are in shallow contact (i.e. fill-out factors  $f < 20\%$ ). Only 4 USPCBs have deep fill-out factors

---

<sup>1</sup>Yunnan Observatories, Chinese Academy of Sciences, 396 Yangfangwang, Guandu District, Kunming, 650216, P. R. China (e-mail: LiuL@ynao.ac.cn)

<sup>2</sup>Key Laboratory for the Structure and Evolution of Celestial Objects, Chinese Academy of Sciences, 396 Yangfangwang, Guandu District, Kunming, 650216, P. R. China

<sup>3</sup>Center for Astronomical Mega-Science, Chinese Academy of Sciences, 20A Datun Road, Chaoyang District, Beijing, 100012, P. R. China

<sup>4</sup>University of Chinese Academy of Sciences, Yuquan Road 19#, Sijingshang Block, 100049 Beijing, China

<sup>5</sup>Facultad de Ciencias Astronómicas y Geofísicas, Universidad Nacional de La Plata, 1900 La Plata, Buenos Aires, Argentina

<sup>6</sup>Instituto de Astrofísica de La Plata (CCT La Plata-CONICET, UNLP), Argentina

<sup>7</sup>National Research Institute of Astronomy and Geophysics, Department of Astronomy, Helwan, Cairo, Egypt

<sup>†</sup>Visiting Astronomer, Complejo Astronómico El Leoncito, operated under agreement between the Consejo Nacional de Investigaciones Científicas y Técnicas de la República Argentina and the National Universities of La Plata, Córdoba, and San Juan

(i.e.  $f > 50, \%$ ). being 1SWASP J200059.78+054408.9, one of them. Generally, contact binaries with deep fill-out factors are going to merge, but it is believed that USPCBs have just evolved to a contact phase. Hence, the deep USPCB 1SWASP J200059.78+054408.9 seems to be a contradiction, making it very interesting. Particularly, 1SWASP J030749.87–365201.7 is a zero contact binary within thermal equilibrium, implying that it should be a turn-off sample as predicted by the thermal relaxation oscillation (TRO) theory.

*Subject headings:* binaries : eclipsing – Stars: individuals (1SWASP J030749.87–365201.7, 1SWASP J213252.93–441822.6, 1SWASP J200059.78+054408.9) – Stars: evolution

## 1. Introduction

W UMa-type contact binaries are usually composed by two cool main sequence stars, where both components are covered by a common convective envelope (CCE). The short-period limit of this type of binaries is an unquestioned fact, and there are some ideas to explain this limitation: (1) the components become fully convective below a certain period (e.g. Rucinski 1992, 1997; Paczyński et al. 2006; Becker et al. 2011) so that the system becomes unstable; (2) the timescale of the angular momentum loss (AML) is much longer than the age of the universe, so that the ultrashort-period eclipsing binary (USPCB) state cannot be achieved (Stępień 2006, 2011). Almost fully convective structure makes USPCBs to be different from the F, G and K type contact binaries.

In recent years, many USPCBs have just been found with the exoplanet searching projects (a list with the names of these surveys was introduced by Koen et al. 2016). Norton et al. (2011) published a catalogue of 53 ultrashort-period eclipsing binary (USPEB) candidates, while Lohr et al. (2013a) investigated the period changes of 143 USPEBs, based on the data of Super Wide Angle Search for Planets (SuperWASP). Koen et al. (2016) confirmed 29 USPEB systems being in overcontact configuration according to a preliminary Fourier decomposition analysis. A series of studies on individual USPCBs have been done in the last 5 years (e.g. Dimitrov & Kjurkchieva 2015; Qian et al. 2015a; Liu et al. 2015a; Jiang et al. 2015a). These studies showed that most USPCBs have shallower fill-out factors ( $f < 20 \%$ ) indicating that USPCBs are in the beginning phase of the contact configuration. Also, some USPCBs have already broken the known short-period limitation or low-mass limitation (e.g., SDSS J001641–000925, Davenport et al. 2013; Qian et al. 2015b). The special USPCBs that are under the critical conditions are interesting and important to understand the evolutionary boundary conditions.

Thus, for this purpose, we observed the following USPCB candidates: 1SWASP J030749.87–365201 (hereafter J030749), 1SWASP J213252.93–441822.6 (hereafter J213252) and 1SWASP J200059.78+0544 (hereafter J200059), with 2-meter-class telescopes. J030749 was discovered by Norton et al. (2011), while J213252 and J200059 were discovered by Lohr et al. (2013a). The period of these three systems are: 19584.393 s (0.22667122 day), 19114.669 s (0.22123459 day) and 17771.663 s (0.20569054 day), respectively (Lohr et al. 2013a). In the literature and in the surveys databases, the light curves of these three USPCBs show very large scatters. So, in this paper, we analyzed these systems with our new observed high-precision multi-color light curves. We report here that the zero contact J030749 and the deep contact J200059, are such special samples mentioned above.

## 2. Observation and data reduction

The southern targets J030749 and J213252 were observed using the 2.15 m Jorge Sahade telescope (JST) at Complejo Astronómico El Leoncito Observatory (CASLEO), San Juan, Argentina. The JST was equipped with a Versarray 2048B-Princeton Instruments CCD camera at the Cassegrain focus, covering a  $5\times 5$  arcmin<sup>2</sup> field of view. The CCD was cooled with liquid nitrogen and a  $5\times 5$  pixel binning factor was applied to enhance the signal-to-noise ratio and to reduce the exposure times. A standard *BVRI* filter set was used. Thus, direct images of J030749 were acquired from November 24 to December 4, 2014, while new images of J213252 were acquired in September 11, 2015.

The new *VRI* images of J200059 were taken in August 1, 2016, with the 1.88 m reflector telescope at the Kottamia Observatory, Astronomy Department, National Research Institute of Astronomy and Geophysics (NRIAG), 11421 Helwan, Cairo, Egypt. A  $2048\times 2048$  pixels EEV CCD 42-40 camera was attached at the Newtonian focus of the telescope, reaching a  $10\times 10$  arcmin<sup>2</sup> field of view. The CCD was also cooled by liquid nitrogen. A summary of the observations can be found in Table 1.

Bias subtraction and flat-fielding corrections were applied to the images in the standard way by means of the IRAF<sup>1</sup> facilities. Subsequent aperture photometry was performed to the targets and the other reference stars to get the differential photometry. The typical errors in the differential photometry are about 0.009 mag for J030749, 0.007 mag for J213252, and 0.006 mag for J200059.

---

<sup>1</sup>IRAF is written and supported by the National Optical Astronomy Observatories (NOAO) in Tucson, Arizona. NOAO is operated by the Association of Universities for Research in Astronomy (AURA), Inc. under cooperative agreement with the National Science Foundation

Finally, the light curves were made up and they are shown in Fig 1. The phases were calculated with the following ephemeris: a)  $2456994.77031 + 0^d.22667122 \times E$  for J030749, b)  $2457276.57884 + 0^d.22123459 \times E$  for J213252, and c)  $2457604.37104 + 0^d.20569054 \times E$  for J200059.

### 3. Light curves solutions

To determine the photometric elements and to understand the geometrical structure and evolutionary state of these three USPCBs, we analyzed their multi-color light curves using the latest version of the Wilson-Devinney (W-D) code (Wilson & Devinney 1971; Wilson 1979, 1990, 2008, 2012; van Hamme & Wilson 2007; Wilson et al. 2010; Wilson & van Hamme 2014).

Usually, the effective temperatures are estimated by colors. At the beginning, we estimated the  $T_1$  (effective temperature of the hot component) based on the  $JHK$  color indexes because our targets have late spectral types (red color). The corresponding  $JHK$  magnitudes (2MASS catalogue, Cutri et al. 2003) are listed in Table 2. The effective temperatures are computed by the method of Worthey & Lee (2011). Then, we applied the  $q$ -searching method to find an initial  $q$  as the input parameter for the W-D code. Such  $q$ -searching grid method is just aimed to make the program to converge faster. In other words, the advantage of the  $q$ -searching method is to save computing time. The results of  $q$ -searching are displayed in Fig 2. The red crosses are the suggested values of  $q$  for each system. For the solutions, the bolometric albedos  $A_1 = A_2 = 0.5$  (Rucinski 1969) and gravity-darkening coefficients  $g_1 = g_2 = 0.32$  (Lucy 1967) were assumed, as it corresponds to a common convective envelope of both components. Square root limb-darkening coefficients were used, according to Claret & Gimenez (1990). The adjustable parameters were: the mass ratio  $q$ ; the orbital inclination  $i$ ; the potential  $\Omega$  (because every solution finally converged to mode 3); the mean temperature of star 2,  $T_2$ ; the monochromatic luminosity of star 1.

However, all light curves showed O’Connell effects (O’Connell 1951). The presence of cool spots on the more massive component can simulate the light curves very well, and it is supported by: i) late type stars have deep convective zones so that they have strong magnetic fields; ii) fast rotate late type stars should have stronger magnetic fields than normals (Barnes & Collier Cameron 2001; Barnes et al. 2004); iii) the more massive component has a deeper convective zone than the less massive one (Mullan 1975). For J030749 the situations of the cool spots are more complicated, being supported by its  $I$ -band night-to-night variations in the light curves (Fig 3). Three cool spots are added to simulate its light curves. One is on the less massive component and two spots are on the more massive component. So

many spots on J030749 suggest that it has very strong magnetic activities. Emphatically, the longitudes of spots can be constrained exactly by the distortions in the light curves. Nevertheless, the other three parameters: latitudes, radii and temperature ratios, are not independent. A very recent study of cool spots on M dwarfs revealed that the fractus cool spots occurred at high latitudes with high frequency (Barnes et al. 2015), according to the doppler maps. Although our model with cool spots is probably, the differential of results with and without cool spots is usually less than 10% (e.g. Qian et al. 2011, 2013a).

Finally, the light curve solutions are listed in Table 3 and the elements of the assumptive cool spots are listed in Table 4. The corresponding fittings of each light curve are shown in Fig 1, and their are shown in Fig 4. The differential color diagrams are shown in Fig ?? . In this figure, it is clearly seen that the colors of the systems vary with the phases, like their light curves. Particularly, there is a swell in the color curves of J030749 around the phase 0.40. This swell means a higher temperature. The amplitude of the color curves suggests an uncertainty of 700 K for the temperature estimation, but it does not change any uncertainty of the temperature ratio ( $T_1/T_2$ ). At last, the geometric constructions of the three USPCBs and the present cool spots are displayed in Fig 6.

#### 4. Discussion of the solutions

In this section, we will mainly discuss about the reliability of the photometric adjustments and the evolutionary states revealed by these solutions. The resulting inclinations for the three systems are greater than 75 degree, strongly indicating that their photometric mass ratios are similar to their spectroscopic mass ratios (Maceroni & van't Veer 1996). Hence, the photometric mass ratios of our solutions should be acceptable. The solutions also show that these three systems are in contact phase, with moderate mass ratios. However, the shortest period system J200059, has a deep contact factor of 58.4%.

Deep USPCBs are very few. This fact is supported both by observational evidence and by theory. The 27 well-studied USPCBs ( $P < 0.24$  day) are collected in Table 5. Only 4 of these 27 USPCBs have deep fill-out factors ( $f > 50\%$ ), while other 16 systems are shallow contact ( $f < 20\%$ ). Unlike the F and G type contact binaries, none of their mass ratios are less than 0.3. Generally, shallow contact factor implies an early phase of contact. According to the thermal relaxation oscillation (TRO) theory (Lucy 1976; Flannery 1976; Webbink 1977), the material flow starts when the primary component (donor) fully filled its Roche lobe, making the orbit shrink, and then, the secondary component (accretor) fully fills its Roche lobe too. The accretor will expand continuously while it accepts mass, making the orbit wider until the contact configuration is broken. Subsequently, the orbit will shrink

again with the mass transfer from the primary to the secondary component. It forms a cycle of contact-semidetached-contact states. In these cycles, the temperatures of the two components will be similar because of the thermal exchange with the mass transfer. The fill-out factor cannot reach high when the system undergoes the TRO cycle because of the existence of the contact broken phase. Therefore, TRO explains why it is such high fraction of shallow USPCBs (16 of 27 systems). For this reason, the zero contact binary within thermal equilibrium J030749, should be in the turn-off phase of the TRO cycle. On the other hand, however, the TRO theory cannot explain the presence of the deep USPCBs with high or moderate mass ratios (e.g., J200059).

If the USPCBs reach a deep fill-out factor, a rapid orbit shrinking mechanism is required. Angular momentum loss (AML) caused by the magnetic stellar winds (e.g. Stępień 2006, 2011) may be the mechanism. He pointed out that if there is a third body or the system is located in a dense field, it could lose a lot of AM. An excessive AML can also occurred in the pre-main-sequence phase. In that time, he mentioned that these possibilities, especially the last one, are quite rare according to the observations (Stępień 2006). However, some studies showed that the presence of third bodies is not very rare (e.g., Pribulla & Rucinski 2006; D’Angelo et al. 2006; Rucinski et al. 2007; Qian et al. 2013b, 2015b). Maybe, the few deep USPCBs in Table 5, including J200059, are formed by the rare AML way, e.g., interaction with third bodies.

## 5. Global parameters correction of the ultrashort-period contact binaries

The physical parameters of close binaries are sufficiently different from the singles or wide binaries because of the strong inter-gravity. For example, the surface gravity accelerations of the components in contact binaries systems are observably lower than those of the same masses single main-sequence stars. Hence, to obtain these parameters for close binaries independently, is very important to build an improved evolutionary model for them. It is predicted that USPCBs have a well empirical global parameter relation than that of F, G and early K type contact binaries because most of them are near the zero age main sequence and/or unevolved. This feature is good for estimating the parameters of USPCBs when it lacks of spectroscopic data. Dimitrov & Kjurkchieva (2015) had already summarized a relationship between the period and the semi-major axis, based on the 14 well-studied binaries with  $P < 0.27$  d ( $a = -1.154 + 14.633 \times P - 10.319 \times P^2$ ). However, one point deviated from this relation, i.e., GSC 1387-0475. It was first investigated by Rucinski & Pribulla (2008) who obtained a spectroscopic mass ratio. Unfortunately, their photometric light curve was not of a good quality. Yang et al. (2010) observed this system again and obtained their

*BVR*-bands light curves. They adopted the spectroscopic mass ratio given by Rucinski & Pribulla (2008), and found smaller masses for the components than theirs. We assumed that this disagreement between both results is caused by the deep fill-out factor. Consequently, we realized that the semi-major axis is probably over estimated with the relation of Dimitrov & Kjurkchieva (2015) when the fill-out factor is huge (e.g.  $f > 50\%$ ). According to the well known Roche potential,

$$\psi = \frac{2}{1+q} \cdot \frac{1}{r_1} + \frac{2q}{1+q} \cdot \frac{1}{r_2} + \left(x - \frac{q}{1+q}\right)^2 + y^2 \quad (1)$$

where  $r_1^2 = x^2 + y^2 + z^2$ ,  $r_2^2 = (1-x)^2 + y^2 + z^2$ ,  $q = M_2/M_1$ ,  $xyz$  are normalized coordinates (with semi-major axis,  $A$ ), and

$$f = \frac{\psi - \psi_{\text{in}}}{\psi_{\text{out}} - \psi_{\text{in}}}, \quad (2)$$

is the fill-out factor definition, we computed the  $r_{\text{side}}$ ,  $r_{\text{back}}$  and  $r_{\text{pole}}$  with a certain fill-out factor  $f$  and mass ratio  $q$ . The effective radius is calculated by  $r_{\text{E}} = \sqrt[3]{r_{\text{side}} \cdot r_{\text{back}} \cdot r_{\text{pole}}}$ . Then, we compared this  $r_{\text{E}}$  to  $r_{\text{L}}$

$$r_{\text{L}} = \frac{0.49q^{-2/3}}{0.6q^{-2/3} + \ln(1 + q^{-1/3})}. \quad (3)$$

which was yielded by Eggleton (1983) with an error less than 1%. Finally, we obtained a ratio of these two normalized radii and used it to correct the semi-major axis. The corresponding results are list in Table 6. All errors list in this table are estimated with the error propagation formula. We found that the masses of GSC 1387-0475 are high close to the values of Yang et al. (2010) after the correction. If we adopt the corrections for J200059, we find that it can be composed of two M type components with mass  $0.458 \pm 0.066 M_{\odot}$  and  $0.199 \pm 0.033 M_{\odot}$ , respectively.

## 6. Conclusions

J030749 is a zero contact binary, with  $q = 0.439 \pm 0.003$  and  $f = 0.0 \pm 3.6\%$ , placed on the turn-off phase of the TRO cycle. J213252 is a shallow contact binary with  $q = 0.560 \pm 0.003$  and  $f = 14.2 \pm 1.9\%$ , under the TRO control. J200059 is a deep contact binary, with  $q = 0.436 \pm 0.008$  and  $f = 58.4 \pm 1.8\%$ . It should be formed by a rapid AML mechanism. The three targets show strong magnetic activities. In summary, J030749 and J200059 are in particular evolutionary stages. It is worth to monitor them in the future.

We thank Allen W. Shafter for giving us constructive suggestions that improved the paper greatly.

This work is partly supported by the Yunnan Natural Science Foundation (2016FB004), the young academic and technology leaders project of Yunnan Province (No. 2015HB098), Chinese Natural Science Foundation (Nos. 11403095 and 11325315), the Key Research Programme of the Chinese Academy of Sciences (grant No. KGZD-EW-603), and Strategic Priority Research Programme “The Emergence of Cosmological Structures” of the Chinese Academy of Sciences (No.XDB09010202). The new observations were made with the telescopes at Complejo Astronómico El Leoncito Observatory (CASLEO), San Juan, Argentina, and the Kottamia Observatory, National Research Institute of Astronomy and Geophysics, Helwan, Cairo, Egypt.

## REFERENCES

- Barnes, J. R., & Collier Cameron, A. 2001, MNRAS, 326, 950
- Barnes, J. R., James, D. J., & Cameron, A. C. 2004, MNRAS, 352, 589
- Barnes, J. R., Jeffers, S. V., Jones, H. R. A., Pavlenko, Ya. V., Jenkins, J. S., Haswell, C. A., Lohr, M. E. 2015, ApJ, 812, 42
- Becker, A. C., Bochanski, J. J., Hawley, S. L., et al. 2011, ApJ, 731, 17
- Claret, A., and Gimenez, A., 1990, A&A 230, 412
- Cutri, R. M. et al. 2003, yCat, 2246, 0
- D’Angelo, C., van Kerkwijk, M. H., Rucinski, S. M. 2006, AJ, 132, 650
- Davenport, J. R. A., Becker, A. C., West, A. A. 2013, ApJ, 764, 62
- Dimitrov D. P. & Kjurkchieva D. P. 2015, MNRAS, 448, 2890
- Djurasevic G., Yilmaz M., Basturk O., Kilicoglu T., Latkovic O., Caliskan S. 2011, A&A, 525, 66
- Eggleton, P. P. 1983, ApJ, 268, 368.
- Elkhateeb, M. M., Saad, S. M., Nouh, M. I., & Shokry, A. 2014a, NewA, 28, 85
- Elkhateeb, M. M., Nouh, M. I., Saad, S. M., & Zaid, I. 2014b, NewA, 32, 10
- Essam, A., Djurašević, G., Ahmed, N. M., & Jurković, M. 2014, NewA, 32, 16
- Flannery, B. P. 1976, ApJ, 205, 217



- Jiang L.-Q., Qian S.-B., Zhang J. and Zhou X. 2015a, *AJ*, 149, 169
- Jiang L., Qian S.-B. and Zhang J. 2015b, *RAA*, 15, 2237
- Jiang L.-Q., Qian S.-B., Zhu L.-Y., Zhang J. and Zhou X. 2015c, *NewA*, 41, 22
- Jiang L., Qian S.-B., Zhang J. and Liu N. 2015d, *PASJ*, 67, 118
- Köse O., Kalomeni B., Keskin V., Ulaş B. and Yakut K. 2011, *AN*, 332, 626K
- Koen C., Koen T., Gray R. O. 2016, *AJ*, 151, 168
- Koen, C. 2014, *MNRAS*, 441, 3075
- Liu, L., Chen, W. P., Qian, S. B., et al. 2015a, *AJ*, 149, 111
- Liu, N.-P., Qian, S.-B., Soonthornthum, B., Zhu, L.-Y., Liao, W.-P., Zhao, E.-G., Zhou, X. 2015b, *AJ*, 149, 148
- Lohr, M. E., Norton, A. J., Kolb, U. C., et al. 2013, *A&A*, 549, A86
- Lohr, M. E., Norton, A. J., Kolb, U. C., & Boyd, D. R. S. 2013, *A&A*, 558, A71
- Lohr, M. E., Hodgkin, S. T., Norton, A. J., & Kolb, U. C. 2014, *A&A*, 563, A34
- Lucy, L. B., 1967, *Zeitschrift für*
- Lucy, L. B. 1976, *ApJ*, 205, 208
- Maceroni, C., & van't Veer, F. 1996, *A&A*, 311, 523
- Mullan, D. J. 1975, *ApJ*, 198, 563
- Norton, A. J., Payne, S. G., Evans, T., et al. 2011, *A&A*, 528, A90
- O'Connell, D. J. K. 1951, *Publications of the Riverview College Observatory*, 2, 85
- Paczyński, B., Szczygieł, D. M., Pilecki, B., & Pojmański, G. 2006, *MNRAS*, 368, 1311
- Pribulla, T., Rucinski, S. M. 2006, *AJ*, 131, 2986
- Qian, S.-B., Liu, L., Zhu, L.-Y., He, J.-J., Yang, Y.-G., Bernasconi, L. 2011, *AJ*, 141, 151
- Qian, S.-B., Liu, N.-P., Li, K. et al. 2013a, *ApJS*, 209, 13
- Qian, S.-B., Zhang, J., Wang, J.-J. et al. 2013b, *ApJS*, 207, 22

- Qian, S. B., Zhang, B., Soonthornthum, B. et al. 2015a, *AJ*, 150, 117
- Qian, S.-B., Jiang, L.-Q., Fernández Lajús, E. et al. 2015b, *ApJ*, 798L, 42
- Rucinski, S. M., & Pribulla, T. 2008, *MNRAS*, 388, 1831
- Rucinski, S. M., Pribulla, T., van Kerkwijk, M. H. 2007, *AJ*, 134, 2353
- Rucinski, S. M., 1969, *A&A* 19, 245
- Rucinski, S. M. 1992, *AJ*, 103, 960
- Rucinski, S. M. 1997, *MNRAS*, 382, 393
- Samec, R. G., Faulkner, D. R., Williams, D. B. 2004, *AJ*, 128, 2997
- Stępień, K. & Gazeas, K. 2012, *AcA*, 62, 153
- Stępień K. 2006, *AcA*, 56, 199
- Stępień K. 2011, *AcA*, 61, 139
- Tout, C. A., & Hall, D. S. 1991, *MNRAS*, 253, 9
- Webbink, R. F. 1977, *ApJ*, 211, 881
- Wilson, R. E., & Devinney, E. J. 1971, *ApJ*, 166, 605
- Wilson, R. E., & van Hamme, W. 2014, *ApJ*, 780, 151
- Wilson, R. E., Van Hamme, W., & Terrell, D. 2010, *ApJ*, 723, 1469
- Wilson, R. E. 1979, *ApJ*, 234, 1054
- Wilson, R. E. 1990, *ApJ*, 356, 613
- Wilson, R. E. 2008, *ApJ*, 672, 575
- Wilson, R. E. 2012, *AJ*, 144, 73
- Worthey, G., & Lee, H.-C. 2011, *ApJS*, 193, 1
- Yang, Y.-G., Wei, J.-Y., Li, H.-L. 2010, *NewA*, 15, 155
- B. Zhang, S. B. Qian, Z. Miloslav, L. Y. Zhu, N. P. Liu, 2017, *NewA*, 54, 52
- Van Hamme, W., & Wilson, R. E. 2007, *ApJ*, 661, 1129

---

This preprint was prepared with the AAS L<sup>A</sup>T<sub>E</sub>X macros v5.2.

Table 1: Summary of the observations.

Target	Obs Date	Texp (s)	Filter	N Img	Telescope	Seeing (")
1SWASP J030749.87–365201.7	2014-11-24	30	I	471	2.15 m JST	3.0-7.0
	2014-11-25	30	I	440	2.15 m JST	3.5-7.5
	2014-12-03	30	V	669	2.15 m JST	3.5-7.5
	2014-12-04	60	B	325	2.15 m JST	3.5-7.0
1SWASP J213252.93–441822.6	2015-09-11	60	R	308	2.15 m JST	3.4-7.4
1SWASP J200059.78+054408.9	2016-08-01	200	V	49	1.88 m KRT	3.0-6.5
	2016-08-01	135	R	46	1.88 m KRT	3.0-6.5
	2016-08-01	170	I	46	1.88 m KRT	3.0-6.5

Table 2: The JHK magnitudes for the targets, comparisons and check stars. Estimated temperatures of the primary components for the three USPCBs based on the JHK colors.

Name	J (mag)	H (mag)	K (mag)	J-K	Type	$T_p$ (K)
1SWASP J030749.87–365201.7	13.552	13.007	12.887	0.665	Target	4750
2MASS J03075380–3653319	12.840	12.407	12.359	0.481	Comparison	
2MASS J03075601–3652174	15.165	14.910	14.873	0.292	Check	
1SWASP J213252.93–441822.6	14.299	13.667	13.622	0.677	Target	4700
2MASS J21325995–4418032	12.782	12.317	12.228	0.554	Comparison	
2MASS J21330002–4418197	13.652	13.263	13.178	0.474	Check	
1SWASP J200059.78+054408.9	13.412	12.875	12.764	0.648	Target	4800
2MASS J20011488+0543026	13.519	13.162	13.048	0.471	Comparison	
2MASS J20011491+0542524	13.420	13.204	13.225	0.195	Check	

Table 3: Photometric solutions for the three USPCBs.

	1SWASP J030749.87–365201.7		1SWASP J213252.93–441822.6		1SWASP J200059.78+054408.9	
Parameters	Photometric elements	errors	Photometric elements	errors	Photometric elements	errors
$g_1 = g_2$	0.32	assumed	0.32	assumed	0.32	assumed
$A_1 = A_2$	0.50	assumed	0.50	assumed	0.50	assumed
$x_{1bolo} = x_{2bolo}$	0.315	assumed	0.315	assumed	0.311	assumed
$y_{1bolo} = y_{2bolo}$	0.371	assumed	0.370	assumed	0.377	assumed
$x_{1V} = x_{2B}$	1.036	assumed	–	–	–	–
$y_{1V} = y_{2B}$	–0.216	assumed	–	–	–	–
$x_{1V} = x_{2V}$	0.682	assumed	–	–	0.658	assumed
$y_{1V} = y_{2V}$	0.135	assumed	–	–	0.162	assumed
$x_{1R} = x_{2R}$	0.423	assumed	0.437	assumed	0.407	assumed
$y_{1R} = y_{2R}$	0.343	assumed	0.330	assumed	0.360	assumed
$x_{1I} = x_{2I}$	0.258	assumed	–	–	0.247	assumed
$y_{1I} = y_{2I}$	0.423	assumed	–	–	0.433	assumed
Phase shift	–	–	–	–	0.0032	$\pm 0.0006$
$T_h$ (K)	4750	$\pm 700$	4700	$\pm 400$	4800	$\pm 300$
$T_c$ (K)	4697	$\pm 703$	4671	$\pm 405$	4528	$\pm 316$
$q = M_c/M_h$	2.280	$\pm 0.010$	1.785	$\pm 0.007$	2.296	$\pm 0.040$
$\Omega_{in}$	5.6432	–	4.9443	–	6.4432	–
$\Omega_{out}$	5.0383	–	4.3545	–	5.8264	–
$\Omega_1 = \Omega_2$	5.6431	$\pm 0.0220$	2.0763	$\pm 0.0033$	5.3123	$\pm 0.0112$
$i$ ( $^\circ$ )	78.2	$\pm 0.1$	81.9	$\pm 0.1$	75.3	$\pm 0.5$
$L_1/(L_1 + L_2)(B)$	0.3415	$\pm 0.0015$	–	–	–	–
$L_1/(L_1 + L_2)(V)$	0.3231	$\pm 0.0012$	–	–	0.4196	$\pm 0.0067$
$L_1/(L_1 + L_2)(R)$	0.3035	$\pm 0.0010$	0.3789	$\pm 0.0013$	0.3975	$\pm 0.0054$
$L_1/(L_1 + L_2)(I)$	0.2801	$\pm 0.0009$	–	–	0.3850	$\pm 0.0048$
$r_1(pole)$	0.2951	$\pm 0.0014$	0.3165	$\pm 0.0012$	0.3200	$\pm 0.0064$
$r_1(side)$	0.3079	$\pm 0.0017$	0.3319	$\pm 0.0015$	0.3392	$\pm 0.0082$
$r_2(back)$	0.3402	$\pm 0.0027$	0.3692	$\pm 0.0025$	0.4027	$\pm 0.0195$
$r_2(pole)$	0.4185	$\pm 0.0013$	0.4124	$\pm 0.0011$	0.4547	$\pm 0.0049$
$r_2(side)$	0.4449	$\pm 0.0016$	0.4386	$\pm 0.0014$	0.4924	$\pm 0.0069$
$r_2(back)$	0.4724	$\pm 0.0021$	0.4704	$\pm 0.0020$	0.5333	$\pm 0.0102$
$f$ (%)	0.0	$\pm 3.6$	14.2	$\pm 1.9$	58.4	$\pm 1.8$

Table 4: Cool spot elements based on the light curve solutions.

		$\theta$ ( $^\circ$ )	$\psi$ ( $^\circ$ )	$\Omega$ (sr)	$T_s/T_*$
1SWASP J030749.87–365201.7	star 1	89.95	157.08	0.35845	0.700
	star 2	86.51	235.49	0.22845	0.850
	star 2	89.95	180.00	0.27845	0.700
1SWASP J213252.93–441822.6	star 2	89.67	77.01	0.20800	0.700
1SWASP J200059.78+054408.9	star 2	89.70	134.30	0.20845	0.700

Table 5: 27 well-studied USPCBs.

Name	Period (day)	$q = M_s/M_p$	$f(\%)$	$i(^{\circ})$	$M_p^*$	$M_s^*$	$R_p^*$	$R_s^*$	reference
1SWASP J030749.87–365201.7	0.2266712	0.439	0.0	78.2	0.789	0.346	0.737	0.507	This paper
RW Com	0.2373464	0.471	6.1	74.9	0.849	0.400	0.774	0.549	Djurasevic et al. (2011)
NSVS 2700153	0.228456	0.775	7.1	47.8	0.650	0.504	0.662	0.589	Dimitrov & Kjurkchieva (2015)
1SWASP J055416.98+442534.0	0.21825	0.792	8.6	70.1	0.582	0.461	0.618	0.556	Dimitrov & Kjurkchieva (2015)
1SWASP J200503.05–343726.5	0.2288836	0.934	9.0	73.8	0.599	0.560	0.637	0.617	Zhang et al. (2017)
1SWASP J160156.04+202821.6	0.22653	0.670	10.0	79.5	0.679	0.455	0.675	0.563	Lohr et al. (2014); Essam et al. (2014)
1SWASP J022727.03+115641.7	0.21095	0.463	10.4		0.659	0.305	0.658	0.464	Liu et al. (2015a)
1SWASP J150822.80–054236.9	0.23006	0.514	12.0	90.0	0.774	0.398	0.729	0.538	Lohr et al. (2014)
1SWASP J074658.62+224448.5	0.22085	0.395	12.6	78.6	0.769	0.304	0.726	0.476	Jiang et al. (2015a)
1SWASP J080150.03+471433.8	0.217531	0.432	13.6	83.8	0.723	0.313	0.698	0.476	Dimitrov & Kjurkchieva (2015)
1SWASP J213252.93–441822.6	0.22123459	0.560	14.2	81.9	0.690	0.386	0.679	0.521	This paper
1SWASP J015100.23–100524.2	0.2145001	0.320	14.6	79.4	0.760	0.243	0.724	0.432	Qian et al. (2015b)
V1104 Her	0.22788	0.623	15.0		0.707	0.441	0.692	0.557	Liu et al. (2015b)
CC Com	0.22068516	0.526	17.0	89.8	0.701	0.369	0.685	0.511	Köse et al. (2011)
SDSS J012119.10C001949.9	0.2052	0.500	18.9	83.9	0.600	0.300	0.622	0.454	Jiang et al. (2015b)
NSVS 7179685	0.20974	0.451	19.3	85.5	0.655	0.295	0.656	0.457	Dimitrov & Kjurkchieva (2015)
NSVS 8626028	0.217407	0.805	20.7	65.9	0.573	0.461	0.612	0.555	Dimitrov & Kjurkchieva (2015)
2MASS J00164102–0009251	0.198561	0.630	22.0	53.3	0.507	0.319	0.564	0.457	Davenport et al. (2013)
1SWASP J024148.62+372848.3	0.21975076	0.813	23.3	68.7	0.585	0.475	0.621	0.565	Jiang et al. (2015c)
1SWASP J133105.91+121538.0	0.21801	0.828	25.2	77.6	0.570	0.472	0.611	0.561	Elkhateeb et al. (2014a)
V523 Cas	0.233693	0.516	29.0	85.4	0.798	0.412	0.744	0.550	Samec et al. (2004)
1SWASP J210318.76+021002.2	0.22859	0.877	34.2	81.9	0.616	0.540	0.645	0.607	Elkhateeb et al. (2014b)
1SWASP J200059.78+054408.9	0.20569054	0.435	58.4	75.3	0.631	0.274	0.642	0.439	This paper
NSVS 925605	0.217629	0.678	70.2	57.2	0.618	0.419	0.637	0.533	Dimitrov & Kjurkchieva (2015)
GSC 1387–0475	0.21781128	0.474	76.3	49.9	0.705	0.334	0.687	0.489	Yang et al. (2010)
1SWASP J075102.16+342405.3	0.20917224	0.740	96.0	76.0	0.543	0.401	0.590	0.514	Jiang et al. (2015d)
1SWASP J234401.81–212229.1	0.21367	0.422		79.4	0.699	0.295	0.683	0.461	Lohr et al. (2013b); Koen (2014)

\* Computed by the relation of Dimitrov & Kjurkchieva (2015) and by equation 3. The footnote P denotes the primary component, while S denotes the secondary component.

Table 6: Semi-major axis corrections for the deep USPCBs.

Name	1SWASP J200059.78+054408.9	NSVS 925605	GSC 1387–0475	1SWASP J075102.16+342405.3
Period (day)	0.20569054	0.21762900	0.21781128	0.20917224
$q = M_s/M_p$	0.436 ± 0.008	0.678 ± 0.003	0.474 ± 0.008	0.740 ± 0.040
$f(\%)$	58.4 ± 1.8	70.2 ± 2.6	76.3 ± 2.9	95.0 ± 4.0
Reference	This paper	Dimitrov & Kjurkchieva (2015)	Yang et al. (2010)	Jiang et al. (2015d)
$a (R_{\odot})$	1.419 ± 0.050	1.542 ± 0.050	1.544 ± 0.050	1.455 ± 0.050
$r_{L1}$	0.452 ± 0.005	0.413 ± 0.004	0.445 ± 0.004	0.405 ± 0.004
$r_{L2}$	0.310 ± 0.003	0.346 ± 0.003	0.316 ± 0.003	0.353 ± 0.004
$r_{E1}$	0.492 ± 0.011	0.475 ± 0.012	0.502 ± 0.012	0.505 ± 0.012
$r_{E2}$	0.352 ± 0.010	0.412 ± 0.010	0.380 ± 0.011	0.467 ± 0.011
$cor = (r_{L1}/r_{E1} + r_{L2}/r_{E2})/2$	0.899 ± 0.013	0.854 ± 0.013	0.860 ± 0.015	0.780 ± 0.010
$a' = a \cdot cor(R_{\odot})$	1.276 ± 0.064	1.317 ± 0.063	1.327 ± 0.066	1.135 ± 0.054
$M_p(M_{\odot})$	0.458 ± 0.066	0.385 ± 0.055	0.448 ± 0.064	0.257 ± 0.031
$M_s(M_{\odot})$	0.199 ± 0.033	0.261 ± 0.038	0.212 ± 0.034	0.190 ± 0.033
$R_p = r_{E1} \cdot a'(R_{\odot})$	0.628 ± 0.046	0.626 ± 0.046	0.666 ± 0.049	0.572 ± 0.041
$R_s = r_{E2} \cdot a'(R_{\odot})$	0.449 ± 0.035	0.543 ± 0.039	0.504 ± 0.040	0.530 ± 0.038

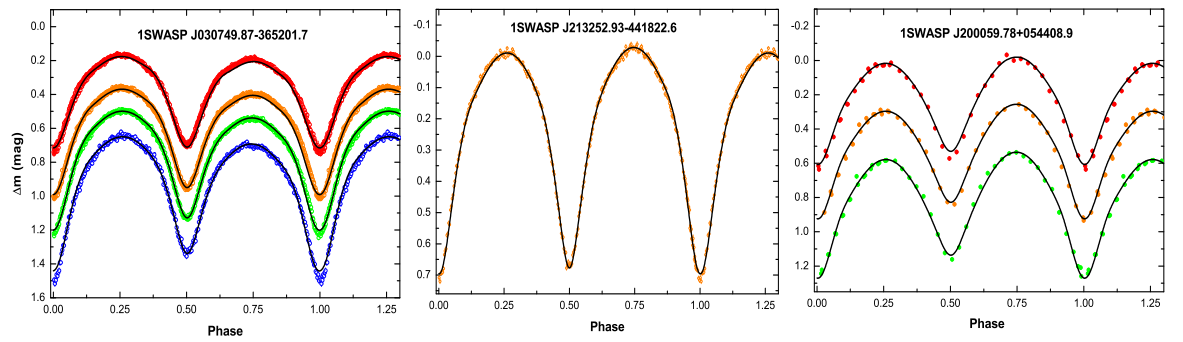


Fig. 1.— Observed and fitted curves for the three USPCBs. The color points denote the observed data with different filters. Blue denotes B filter; green denotes V filter; orange denotes R filter; red denotes I filter. The black solid lines are the theoretical fittings, with the modeling of dark spots.

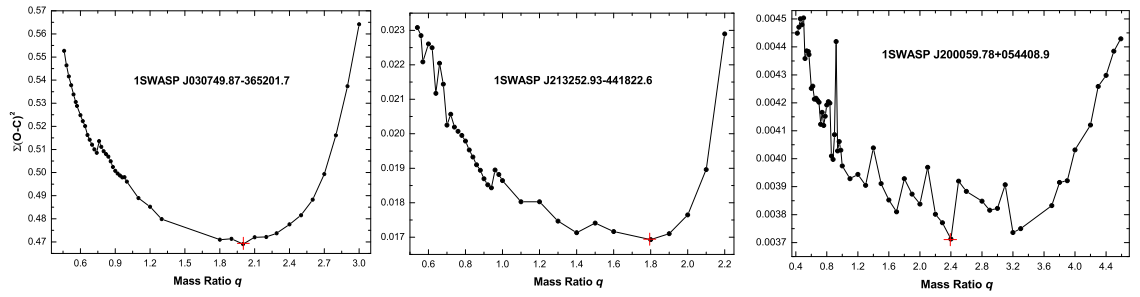


Fig. 2.— The relation between  $q$  and fitting residuals for the three USPCBs. The red cross in each diagram presents the initial value of  $q$  at the beginning of the W-D program running.

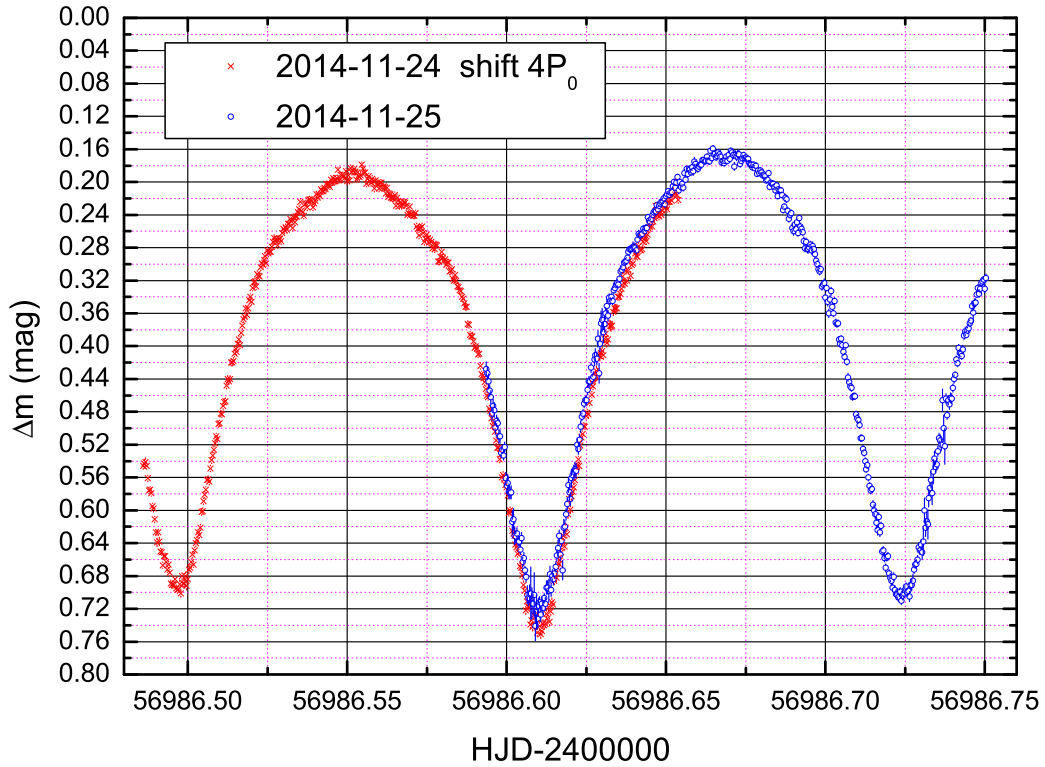


Fig. 3.— The night-to-night light curve variation of 1SWASP J030749.87–365201.7. The red data points were observed on the night of 2014-11-24 with the I filter, while the blue data points were observed on the night of 2014-11-25 with the same filter. We add four times of  $P_0$  (0.2266712 day) to the red points. However, this two parts of light curves do not join well. Moreover, a changing of depths of minima is clear seen. This phenomenon could be caused by variations of the presented cool spots.



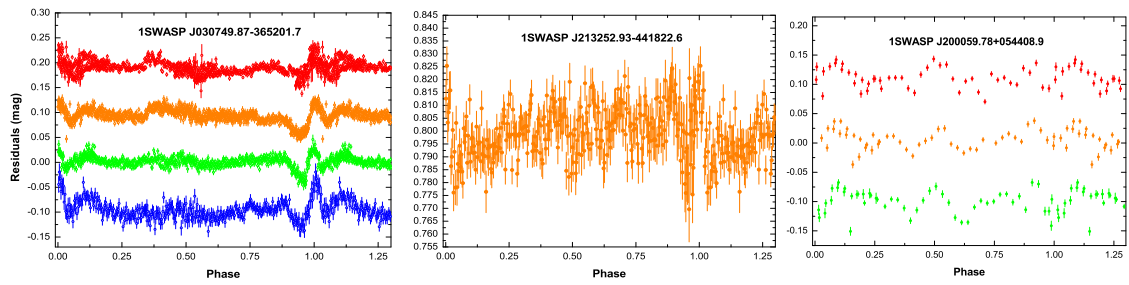


Fig. 4.— Fitting residuals of light curves for the three USPCBs. The colors denote the same meaning as the Fig 1.

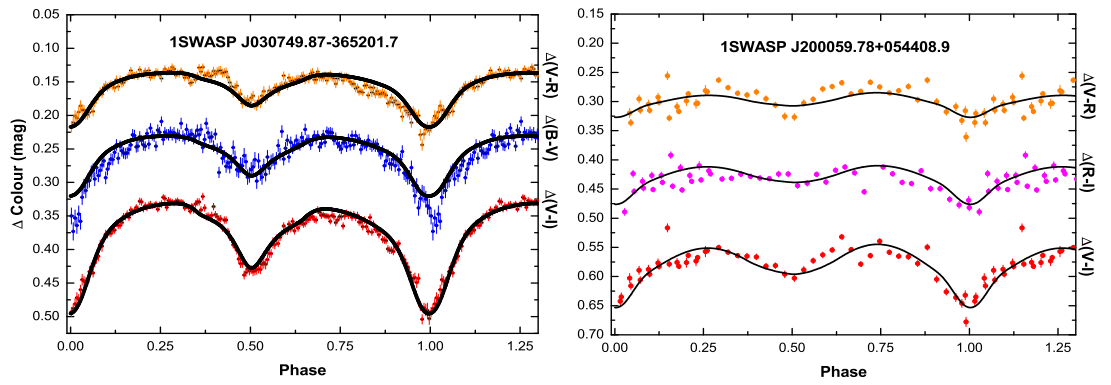


Fig. 5.— Observed differential colors for the three USPCBs. Blue denotes  $\Delta(B-V)$ ; orange denotes  $\Delta(V-R)$ ; red denotes  $\Delta(V-I)$ ; magenta denotes  $\Delta(R-I)$ . The solid lines are yielded by the W-D program.

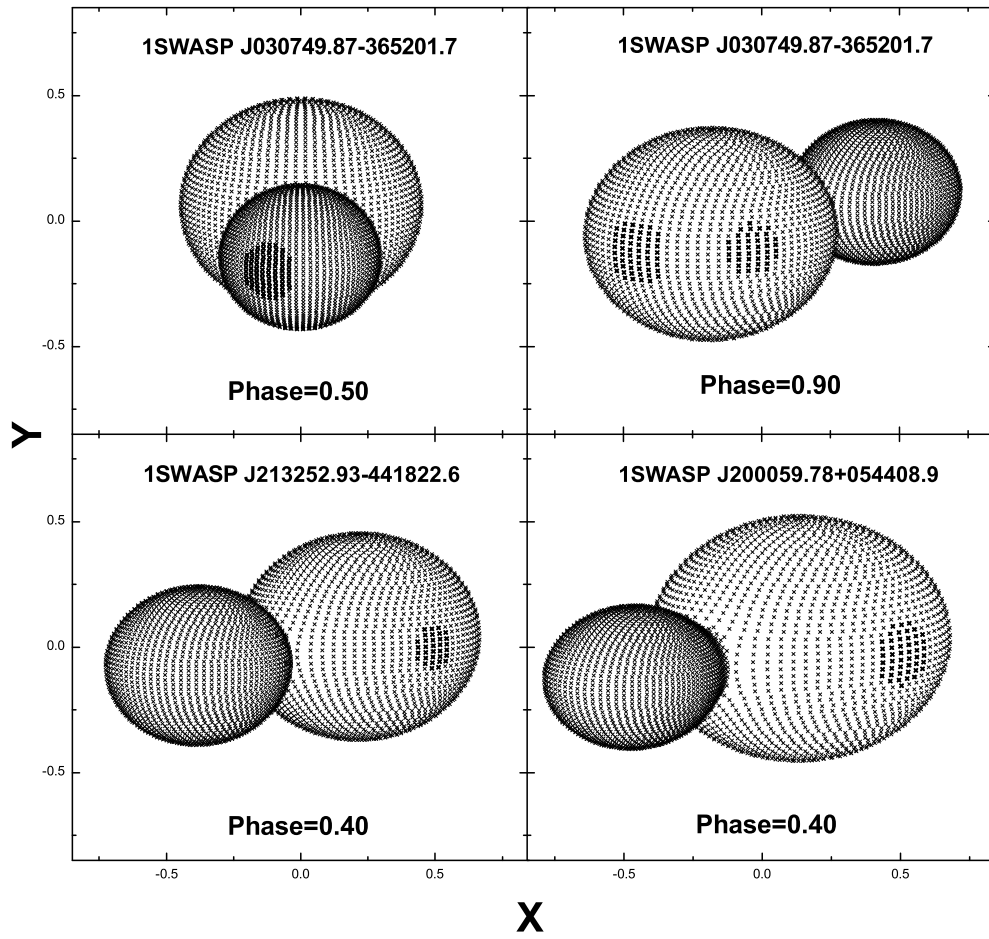


Fig. 6.— The geometrical structure of the three USPCBs with their present cool spots.